

EPFL



LABORATORY OF CRYOSPHERIC SCIENCES (CRYOS)

OpenFOAM Tutorial Project

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**Implementation of an  
Eulerian-Lagrangian snow transport  
model in OpenFOAM:  
*snowBedFoam 1.0***

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Developed for OpenFOAM version 2.3.0.

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## 1 Introduction

The present document describes the implementation of an aeolian snow transport model within the open source computational fluid dynamics (CFD) software OpenFOAM. It was developed in the context of a master thesis at the Ecole Polytechnique Fédérale de Lausanne (EPFL) and the WSL Institute for Snow and Avalanche Research SLF, Switzerland. Two submodels are added to the original OpenFOAM Lagrangian library to simulate the transport of snow particles by the wind, in particular for medium- (saltation) and small-sized (suspension) particles. Herein, we first describe the theoretical framework for snow transport processes and their related mathematical expressions. Then, we present the OpenFOAM scripts embedding the different Lagrangian submodels for snow movement along with the files defining the new solver (*snowBedFoam*). This tutorial aims to make the modelling of snow transport more accessible to the OpenFOAM community.

## 2 Theoretical background

The current knowledge of snow transport processes which contributed to the build-up of our OpenFOAM model is described here. The text was inspired by the candidacy report of [Brito Melo \(2019\)](#), which outlines the main literature findings on the aeolian transport of particles.

### 2.1 Snow transport: general aspects

The early work of [Bagnold \(1941\)](#) constitutes a reference for the aeolian transport of sand. Still, his findings stay relevant to other particles, among which snow and its various interactions with wind. Snow aeolian transport occurs at a wide range of elevations, from regions close to the ground to high altitudes. Three main modes of transport are distinguished based on their underlying physical processes: 1) *saltation*, which describes the motion of particles close to the surface. In this mode, grains follow ballistic trajectories and return to the snow bed, possibly rebounding and/or ejecting other particles; ; 2) *suspension*, which relates to the transport of particles that are sufficiently light to be lifted higher up by turbulent eddies; 3) *creep* (or *reptation*), which is the rolling of heavier particles along the surface due to impacting grains or aerodynamic forces. Its contribution usually stays negligible compared to the other processes ([Vionnet et al., 2013](#)).

The saltation of grains along the surface accounts for about 75% of all particle movement by

wind (Bagnold, 1941). In our OpenFOAM model, both the suspension and saltation modes are represented but saltation stays predominant. Most saltating particles are confined to a thin layer close to the surface ( $\sim 10$  cm), which we refer to as the *saltation layer*. When aloft, saltating particles are accelerated by the fluid flow: their kinetic energy is partly dissipated as friction losses, partly sustained to start a new ballistic trajectory and partly transferred to eject other grains from the snowbed surface. A total of three saltation modes are commonly identified (Figure 1): aerodynamic entrainment, rebound and ejection. *Aerodynamic entrainment* (or lift) occurs when particles initially at the surface are lifted up by aerodynamic forces only. *Rebound* happens when particles bounce to a new ballistic trajectory after hitting the ground. *Ejection* (or splash) occurs when particles laying in the ground are set in motion due to the impact of saltating particles (Doorschot and Lehning, 2002). These transport modes are in fact modes of saltation initiation, which have a great impact on the ballistic trajectory of the particle. Different authors contributed to the physical understanding of these saltation modes and developed parametrizations of the wind-particle-bed interaction. We particularly refer to Comola and Lehning (2017) whose findings were implemented in the snow transport solver described herein.

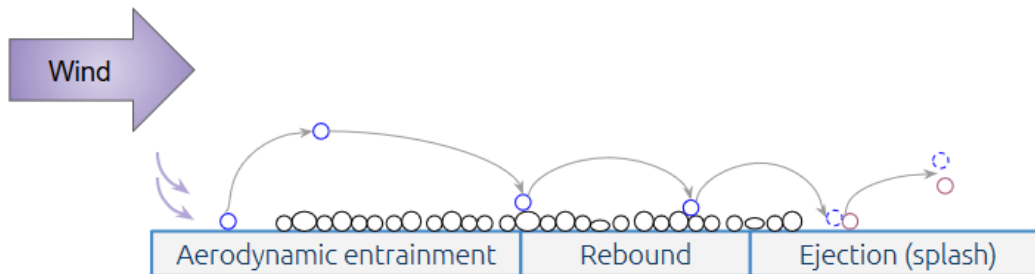


Figure 1: The three main particle saltation modes: aerodynamic entrainment, rebound and ejection. Adapted from Brito Melo (2019).

Based on several wind tunnel experiments with sand of uniform grain size that he conducted, Bagnold (1941) could establish the concept of *fluid threshold* which is the wind speed necessary for grains to start saltating when initially at rest. This threshold value varies in direct proportion to the predominant grain size of the sand surface. Thus, saltation starts when the shear stress exceeds the fluid threshold: this is an important concept for the build-up of our snow movement model. All the related mathematical expressions are detailed in the next subsection.

## 2.2 Governing equations for snow surface-flow interaction

The underlying principles and equations of the OpenFOAM snow transport model are described here. They are similar to those of the Large Eddy Simulation-Lagrangian Stochastic Model (LES-LSM) developed within the CRYOS laboratory at EPFL (CRYOS, 2021). We refer to the work of Comola and Lehning (2017) and Sharma et al. (2018) for more details. The three saltation modes - aerodynamic lift, rebounding and ejection of grains - are represented in the model under a mathematical form and implemented in the scripts in such manner.

### 2.2.1 Aerodynamic entrainment

Grains lying on the snow bed can be entrained into the saltation layer when the fluid surface shear stress  $\tau_{f,surf}$  is large enough to lift them up, namely when it exceeds the fluid threshold value  $\tau_{th}$  defined as (Bagnold, 1941)

$$\tau_{th} = A^2 g \langle d_p \rangle (\rho_p - \rho_f) \quad (1)$$

where  $\langle d_p \rangle$  is the mean particle diameter,  $\rho_p$  and  $\rho_f$  are the particle and fluid densities, respectively and A is an empirical constant taken equal to 0.2 for snow as determined by Clifton et al. (2006) through wind-tunnel experiments.  $g$  refers to the gravitational acceleration and is assumed to be equal to 9.81 m/s<sup>2</sup>.

Two different formulations for surface shear stress were implemented in the OpenFOAM aerodynamic lift submodel. The first one is obtained by applying the logarithmic law of the wall (LOW),

$$\tau_{f,surf}^{LOW} = \rho_f \left( \frac{\kappa |\mathbf{U}_t|}{\ln(z/z_0)} \right)^2 \quad (2)$$

where  $\mathbf{U}_t$  is the tangential velocity vector,  $z$  the height of the first grid cell center,  $z_0$  the aerodynamic roughness length and  $\kappa = 0.41$  the von Kármán constant. The second expression is based on the vertical velocity gradient and the total kinematic viscosity:

$$\tau_{f,surf}^{TKV} = \rho_f \left( \frac{\partial u}{\partial z} \Big|_{z=0} (\nu_t + \nu) \right) \quad (3)$$

where  $\frac{\partial u}{\partial z} \Big|_{z=0}$  is the vertical velocity gradient and  $\nu$ ,  $\nu_t$  the viscous and turbulent kinematic viscosity, respectively. This method has the advantage to be universal and independent of the wall function employed in the simulations. In each grid cell, the number of particles

aerodynamically entrained by the fluid at each timestep,  $N_{ae}$ , linearly increases with the excess shear stress according to the formulation of [Anderson and Haff \(1991\)](#):

$$N_{ae} = \frac{C_e}{8\pi\langle d_p \rangle^2} (\tau_{f,surf} - \tau_{th}) \Delta x \Delta y \Delta t \quad (4)$$

where  $C_e$  is an empirical parameter set to 1.5 ([Doorschot and Lehning, 2002](#)),  $\Delta x$  and  $\Delta y$  are the grid dimensions in the streamwise/spanwise directions and  $\Delta t$  is the simulation timestep. Once that  $N_{ae}$  is determined, particles are launched at height  $h_{init} = 4\langle d_p \rangle$  and the particle diameter, initial velocity magnitude and ejection angle are all sampled from statistical distributions according to [Clifton and Lehning \(2008\)](#). More details can be found in their work.

### 2.2.2 Rebound and splash entrainment

Depending on its path, a snow particle present in the fluid might hit the surface upon which it can not only rebound -defined as *rebound* entrainment- but also eject other particles from the bed to the overlying fluid, defined as *splash* entrainment. The probability  $P_r$  that the snow particle rebounds when impacting the bed is given by [Anderson and Haff \(1991\)](#) as follows

$$P_r = P_m (1 - e^{-\gamma v_i}) \quad (5)$$

where  $P_m$  is the maximum probability equal to 0.9 for snow ([Groot Zwaaftink et al., 2013](#)),  $\gamma$  is an empirical constant equal to 2, and  $v_i$  is the velocity magnitude of the impacting particle. When rebounding, the particle is assumed to have a velocity magnitude of  $v_r = 0.5v_i$  ([Doorschot and Lehning, 2002](#)) and the rebound angle is determined from a statistical distribution according to [Kok and Rennó \(2009\)](#).

Concerning the splash entrainment, the number of particles ejected from the bed  $N_{splash}$  is defined as the minimum between  $N_E$  and  $N_M$  whose expressions are ([Comola and Lehning, 2017](#)):

$$N_E = \frac{(1 - P_r \epsilon_r - \epsilon_{fr}) d_i^3 v_i^2}{2\langle v \rangle^2 (\langle d \rangle + \frac{\sigma_d^2}{\langle d \rangle})^3 \left( 1 + r_E \sqrt{5[1 + (\frac{\sigma_d}{\langle d \rangle})^2]^9 - 5} \right) + 2\frac{\phi}{\rho_p}} \quad (6)$$

$$N_M = \frac{(1 - P_r \mu_r - \mu_{fr}) d_i^3 v_i \cos \alpha_i}{\langle v \rangle^2 (\langle d \rangle + \frac{\sigma_d^2}{\langle d \rangle})^3 \left( \langle \cos \alpha \rangle \langle \cos \beta \rangle r_M \sqrt{[1 + (\frac{\sigma_d}{\langle d \rangle})^2]^9 - 1} \right)} \quad (7)$$

$N_M$  and  $N_E$  are the number of ejections predicted by the momentum and energy balance, respectively. In Eq.6,  $\epsilon_{fr}$  and  $\epsilon_r$  are the fractions of impact energy lost to the bed and kept by the rebounding particle, respectively.  $\mu_{fr}$  and  $\mu_r$  are their equivalent for momentum in Eq.7.  $\langle d \rangle$  and  $\sigma_d$  are the mean and standard deviation of the ejecta's diameter,  $\langle v \rangle$  its mean velocity and  $\alpha$  and  $\beta$  the horizontal and vertical ejection angles.  $\phi$  is the cohesive bond exerted on a particle by its neighboring particles.  $r_M$  and  $r_E$  are correlation coefficients linking mass and velocity. More details about the derivation of these expressions can be found in the work of [Comola and Lehning \(2017\)](#). Similarly to the aerodynamic entrainment, the characteristics of the splashed particles are randomly sampled from statistical distributions. Overall, details about the equations of the surface-flow interaction can be found in the Supplementary Materials of the work from [Sharma et al. \(2018\)](#).

### 3 Implementation of a snow transport model

From this section on, several fonts are employed: the OpenFOAM font refers to the solver and function names of the software; the `command` font is employed when referring to a terminal command and directory/file names.

The existing OpenFOAM solver DPMFoam is employed for the implementation of this new snow transport model. It employs the lagrangian library of the software which compiles a variety of Lagrangian particle tracking (LPT) libraries. DPMFoam is a multiphase flow solver that handles the coupled Eulerian–Lagrangian phases and involves a finite number of particles spread in a continuous phase. The motion of individual particles is obtained directly by solving Newton's second law of motion, which corresponds to the so-called discrete particle method (DPM). Particles are aggregated in clouds and treated as one big computational parcel, where the effect of the volume fraction of particles on the continuous phase is included within the Eulerian continuum equations. Details on the numerical approach employed in DPMFoam are given in [Fernandes et al. \(2018\)](#), along with validation results.

Overall, the following steps must be performed for the build-up of a snow transport model:

1. The implementation of the aerodynamic entrainment equations (Sect.2.2.1) using the stochasticCollision submodel as a base;
2. The implementation of the rebound and splash entrainment modes (Sect.2.2.2) based on the patch-interaction submodel localInteraction;

3. The integration of a source term in the Eulerian momentum equations in the form of a large-scale pressure gradient;
4. The set-up of an initial velocity profile following the logarithmic law to reach faster convergence. Addition of an extra term for random noise is also made possible in order to mimic the effect of turbulence.
5. The addition of so-called volScalarField objects for the visualization of particle deposition and entrainment as well as surface friction velocity at the surface.

The main implementation steps mentioned above are described in details in the following sections. The first step consists in copying into the user folder (`$WM_PROJECT_USER_DIR`) the intermediate and distributionModels directories from the lagrangian library located in the OpenFOAM source libraries directory (`$FOAM_SRC`) through the following command:

```
cp -r $FOAM_SRC/lagrangian/intermediate \  
$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/intermediateCRYOS/
```

Comparably for the distributionModels library:

```
cp -r $FOAM_SRC/lagrangian/distributionModels \  
$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/distributionModelsTriple/
```

It is important that the folders copied in the user folder are named differently than the original ones to avoid compiling issues: here the names `lagrangianCRYOS`, `intermediateCRYOS` and `distributionModelsTriple` can be replaced by any other meaningful terms. Once that the folders are set, the name changes need to be taken into account for the compilation of the modified libraries. At the last line of the file `Make/files` in the respective folders, replace the `$(FOAM_LIBBIN)` expression by `$(FOAM_USER_LIBBIN)` and add the name of the new library:

```
LIB = $(FOAM_USER_LIBBIN)/liblagrangianIntermediateCRYOS  
LIB = $(FOAM_USER_LIBBIN)/libdistributionModelTriple
```

Similarly, the DPMFoam solver folder must be copied from the OpenFOAM applications directory (`$FOAM_APP`) via the command:

```
cp -r $FOAM_APP/solvers/lagrangian/DPMFoam \  
$WM_PROJECT_USER_DIR/applications/solvers/snowDPMFoam
```

Rename the `DPMFoam.C` file to `snowBedFoam.C`. In order to be able to compile the new application, the files must be modified in the `Make` directories. Change



snowDPMFoam/Make/files to

```
DPMNewFoam.C
```

```
EXE = $(FOAM_USER_APPBIN)/snowBedFoam
```

and snowDPMFoam/DPMTurbulenceModels/Make/files to

```
DPMTurbulenceModels.C
```

```
LIB = $(FOAM_USER_LIBBIN)/libDPMTurbulenceModelsNew
```

The implementation stages described hereafter must be carried out in the user folder: by principle, the original OpenFOAM files in \$FOAM\_SRC should never be modified to ensure the correct operation of the software.

### 3.1 Particle statistical distribution models

Before the implementation of the snow transport equations, a new class must be created to integrate the different types of statistical distribution used for the sampling of the dimension, ejection angle and velocity of the particles (described in details in section S1.4. of [Sharma et al. \(2018\)](#), Supplementary Materials). This was achieved by using the OpenFOAM class `distributionModels` as a template. A total of three different statistical distributions are considered, namely: exponential, log-normal and normal. The subsequent step-by-step approach must be followed for their implementation:

1. In the `distributionModelsTriple` directory that was just created in the user folder, delete all the subdirectories except for the ones named `distributionModel` and `exponential`. The `Make` folder should also remain as it is essential for compilation;
2. Replace the term "`distributionModel(s)`" by "`distributionModel(s)Triple`" and "`exponential`" by "`normalLogNormalExponential`" in all the files and folders containing these instances;
3. In the file `distributionModelTriple.C`, delete the content of the `Foam::distributionModels::distributionModel::check()` Protected Member Function and replace the existing Member Functions by `normalSample()`, `logNormalSample()` and `exponentialSample()`. These functions should also be defined in `distributionModelTriple.H`, while the ones that were replaced should be removed. No changes should be brought to `distributionModelTripleNew.C`, except for the name as specified in the first step.

4. In the `normalLogNormalExponential.H` file, delete the lines found under the `Private Data` and `Member Functions` sections and add the definition of the `normalSample`, `logNormalSample` and `exponentialSample` functions;
5. In the `normalLogNormalExponential.C` file, add the mathematical expressions related to the three statistical distribution `Member Functions` used for the sampling of particle properties. In the `Constructors` section, keep only the `distributionModelTriple (p)` variable.

Figures 2-3 and 4-5 show the OpenFOAM \*.H and \*.C scripts for the new `normalLogNormalExponential` class, respectively. The equations corresponding to the statistical distributions are in Figure 5. As a final step, add the following line in the `Make/options` file of the `intermediateCRYOS` folder, after the expression `EXE_INC = \`:

```
-I../distributionModelsTriple/lnInclude \
```

In the same file, add the following after the line containing `LIB_LIBS = \`:

```
-L$(FOAM_USER_LIBBIN) \  
-ldistributionModelTriple
```

These steps are needed for the correct compilation of the new class.

```

1  /*-----*\
2  =====
3  \ \ / / F i e l d           |   OpenFOAM: The Open Source CFD Toolbox
4  \ \ / / O p e r a t i o n   |
5  \ \ / / A n d                |   Copyright (C) 2011-2013 OpenFOAM Foundation
6  \ \ / / M a n i p u l a t i o n |
7  -----*\
8  License
9      This file is part of OpenFOAM.
10
11     OpenFOAM is free software: you can redistribute it and/or modify it
12     under the terms of the GNU General Public License as published by
13     the Free Software Foundation, either version 3 of the License, or
14     (at your option) any later version.
15
16     OpenFOAM is distributed in the hope that it will be useful, but WITHOUT
17     ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or
18     FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License
19     for more details.
20
21     You should have received a copy of the GNU General Public License
22     along with OpenFOAM. If not, see <http://www.gnu.org/licenses/>.
23
24  Class
25      Foam::normalLogNormalExponential
26
27  Description
28      normalLogNormalExponential distribution model
29
30  SourceFiles
31      normalLogNormalExponential.C
32
33  /*-----*/
34
35  #ifndef normalLogNormalExponential_H
36  #define normalLogNormalExponential_H
37
38  #include "distributionModelTriple.H"
39
40  // * * * * *
41
42  namespace Foam
43  {
44      namespace distributionModelsTriple
45      {
46
47          /*-----*\
48                          Class normalLogNormalExponential Declaration
49          /*-----*/
50
51          class normalLogNormalExponential
52          :
53              public distributionModelTriple
54          {
55
56          public:
57

```

Figure 2: normalLogNormalExponential.H, lines 1 to 57.

## Implementation of a snow transport model in OpenFOAM

```
58     //- Runtime type information
59     TypeName("normalLogNormalExponential");
60
61
62     // Constructors
63
64     //- Construct from components
65     normalLogNormalExponential(const dictionary& dict, cachedRandom& rndGen);
66
67     //- Construct copy
68     normalLogNormalExponential(const normalLogNormalExponential& p);
69
70     //- Construct and return a clone
71     virtual autoPtr<distributionModelTriple> clone() const
72     {
73         return autoPtr<distributionModelTriple>(new
74             normalLogNormalExponential(*this));
75     }
76
77     //- Destructor
78     virtual ~normalLogNormalExponential();
79
80
81     // Member Functions
82
83     //- Sample the normal distribution model
84     virtual scalar normalSample(scalar mean_, scalar std_) const;
85
86     //- Sample the lognormal distribution model
87     virtual scalar logNormalSample(scalar mean_, scalar std_) const;
88
89     //- Sample the exponential distribution model
90     virtual scalar exponentialSample(scalar mean_, scalar std_) const;
91
92
93 };
94
95
96 // * * * * *
97
98 } // End namespace distributionModelsTriple
99 } // End namespace Foam
100
101 // * * * * *
102
103 #endif
104
105 // *****
```

Figure 3: normalLogNormalExponential.H, lines 58 to 105.

## Implementation of a snow transport model in OpenFOAM

```

1  /*-----*\
2  =====
3  \ \ / / F i e l d           | OpenFOAM: The Open Source CFD Toolbox
4  \ \ / / O p e r a t i o n   |
5  \ \ / / A n d                | Copyright (C) 2011-2013 OpenFOAM Foundation
6  \ \ / / M a n i p u l a t i o n |
7  -----*\
8  License
9      This file is part of OpenFOAM.
10
11     OpenFOAM is free software: you can redistribute it and/or modify it
12     under the terms of the GNU General Public License as published by
13     the Free Software Foundation, either version 3 of the License, or
14     (at your option) any later version.
15
16     OpenFOAM is distributed in the hope that it will be useful, but WITHOUT
17     ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or
18     FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License
19     for more details.
20
21     You should have received a copy of the GNU General Public License
22     along with OpenFOAM. If not, see <http://www.gnu.org/licenses/>.
23
24  /*-----*\
25
26  #include "normalLogNormalExponential.H"
27  #include "addToRunTimeSelectionTable.H"
28  #include "mathematicalConstants.H"
29
30  // * * * * * Static Data Members * * * * * //
31
32  namespace Foam
33  {
34      namespace distributionModelsTriple
35      {
36          defineTypeNameAndDebug(normalLogNormalExponential, 0);
37          addToRunTimeSelectionTable(distributionModelTriple,           ↗
38                                     normalLogNormalExponential, dictionary);
39      }
40  }
41
42  // * * * * * Constructors * * * * * //
43  Foam::distributionModelsTriple::normalLogNormalExponential::normalLogNormalExponential
44  (
45      const dictionary& dict,
46      cachedRandom& rndGen
47  )
48  :
49      distributionModelTriple(typeName, dict, rndGen)
50  {
51      check();
52  }
53
54
55  Foam::distributionModelsTriple::normalLogNormalExponential::normalLogNormalExponential

```

Figure 4: normalLogNormalExponential.C, lines 1 to 55.

```

56 |   al(const normalLogNormalExponential& p)
57 |   :
58 |     distributionModelTriple(p)
59 |   {}
60 |
61 |   // * * * * * D e s t r u c t o r * * * * * //
62 |
63 |   Foam::distributionModelsTriple::normalLogNormalExponential::~normalLogNormalExponential()
64 |   {}
65 |
66 |
67 |   // * * * * * M e m b e r   F u n c t i o n s   * * * * * //
68 |
69 |   Foam::scalar
70 |   Foam::distributionModelsTriple::normalLogNormalExponential::normalSample(scalar
71 |   mean_, scalar std_) const
72 |   {
73 |     scalar rand1=rndGen_.sample01<scalar>();
74 |     scalar rand2=rndGen_.sample01<scalar>();
75 |     rand1=min(rand1+ROOTVSMALL,1.0);
76 |     scalar
77 |     val=mean_+std_*sqrt(-2.0*log(rand1))*cos(2.0*constant::mathematical::pi*rand2);
78 |     return val;
79 |   }
80 |
81 |   Foam::scalar
82 |   Foam::distributionModelsTriple::normalLogNormalExponential::logNormalSample(scalar
83 |   mean_, scalar std_) const
84 |   {
85 |     scalar s2 = log(1.0+pow(std_/mean_,2.0));
86 |     scalar m = log(mean_) - 0.5*s2;
87 |     scalar rand1=rndGen_.sample01<scalar>();
88 |     scalar rand2=rndGen_.sample01<scalar>();
89 |     rand1=min(rand1+ROOTVSMALL,1.0);
90 |     scalar
91 |     val=m+sqrt(s2)*sqrt(-2.0*log(rand1))*cos(2.0*constant::mathematical::pi*rand2);
92 |     val=exp(val);
93 |     return val;
94 |   }
95 |
96 |   Foam::scalar
97 |   Foam::distributionModelsTriple::normalLogNormalExponential::exponentialSample(scalar
98 |   mean_, scalar std_) const
99 |   {
100 |     scalar rand1=rndGen_.sample01<scalar>();
101 |     rand1=min(rand1,1.0-ROOTVSMALL);
102 |     scalar val = -mean_*log(1.0-rand1);
103 |     return val;
104 |   }
105 |   // * * * * *

```

Figure 5: normalLogNormalExponential.C, lines 56 to 96.

## 3.2 Submodel 1: aerodynamic entrainment

### 3.2.1 Copying the model template

The first step in the implementation of the aerodynamic lift submodel is to copy the stochasticCollision template directory found at:

```
$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/intermediateCRYOS/submodels/...  
Kinematic/StochasticCollision
```

Once this is done, follow the steps:

1. Rename the copied directory `BedAerodynamicLiftInjectionModel`;
2. Rename the `StochasticCollisionModel` subfolder by `BedAerodynamicLiftInjectionModel`. Do the same for all the files located inside. This will be the template of the class that was newly created;
3. Rename the `NoStochasticCollision` folder as well as all the files it contains by `NoBedAerodynamicLiftInjection`;
4. Inside all the files that were renamed in steps 2 and 3, replace the instances of the term "StochasticCollision" by the term "BedAerodynamicLiftInjection".
5. Create a copy of the new `BedAerodynamicLiftInjectionModel` subfolder and rename it `LogLawShearStress`. Inside the latter, replace every instance of the word "StochasticCollisionModel" by "LogLawShearStress" in the \*.C and \*.H files. It is in these scripts that the mathematical base for the aerodynamic lift model will be implemented;

At this stage, in the folder located at the path

```
$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/intermediateCRYOS/submodels/...  
Kinematic/BedAerodynamicLiftInjectionModel
```

You should have the list of directories shown in Figure 6.

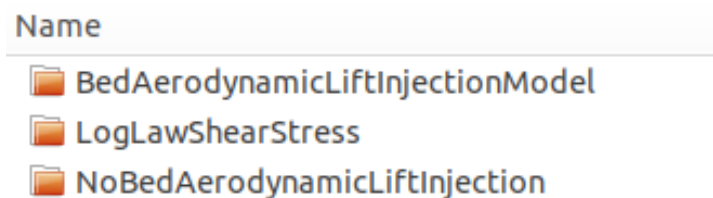


Figure 6: Content of the `BedAerodynamicLiftInjectionModel` directory.

### 3.2.2 Description of the functions

The actual implementation of the aerodynamic entrainment equations can be performed now. Within the files of the three classes that were just created (LogLawShearStress - NoBedAerodynamicLiftInjection - BedAerodynamicLiftInjectionModel), replace the last term of the function

Foam::ClassName<CloudType>::collide(const scalar dt)

by bedAeroLiftInject(). This new function constitutes the base for the implementation of the aerodynamic entrainment equations within the LogLawShearStress class. No other change should be brought to BedAerodynamicLiftInjectionModel and NoBedAerodynamicLiftInjection. In the LogLawShearStress directory, simultaneously open the LogLawShearStress.H and LogLawShearStress.C files. In the new bedAeroLiftInject() function, erase all the lines that were related to the original collide function. Table 1 summarizes the Protected Member Functions involved in the LogLawShearStress model and their utility.

Function	Utility
bedAeroLiftInject	Main routine of the script. For every cell, the surface shear stress is computed and the number of lifted particles determined accordingly.
normallInject	Accounts for the vertical shift of the lifted particles and adds them in the domain (see <a href="#">Sharma et al. (2018)</a> , section S1.4.).

Table 1: Functions implemented in the aerodynamic entrainment model and their utility.

Linking the mathematical expressions from Section 2 to their corresponding segments of the code, the shear stress threshold (Eq.1) is implemented within the bedAeroLiftInject function at line 131 (Fig.12). The shear stress found at the surface can be computed in two ways (to be specified by the user in the kinematicCloudProperties file of the case directory), either by applying the logarithmic law (Eq.2 - line 124, Fig.12) or via the modelled turbulent kinematic viscosity (Eq.3 - line 128, Fig.12). The difference between the threshold and actual surface shear stress is used to determine the number of aerodynamically lifted particles  $N_{ae}$ , at line 135 (Eq.4 - Fig.12). From line 141 on, the code is related to the random sampling of the particle properties as well as to the injection of particles through the call of the respective functions (Table 1).



### 3.2.3 OpenFOAM scripts

The scripts related to our BedAerodynamicLiftInjectionModel Lagrangian submodel and more especially to the LogLawShearStress class are given below. Figures 7 to 9 present extracts from the LogLawShearStress.H file which contain data types and function definitions. The commented lines briefly describe the variables that are employed in the model. Figures 10 to 16 constitute the parts of the LogLawShearStress.C script where the equations for aerodynamic lift were included.

## Implementation of a snow transport model in OpenFOAM

```
1  /*-----*\
2  =====
3  \\      /  F ield      |  OpenFOAM: The Open Source CFD Toolbox
4  \\      /  O peration  |
5  \\      /  A nd        |  Copyright (C) 2011-2013 OpenFOAM Foundation
6  \\      /  M anipulation |
7  -----*\
8  License
9  This file is part of OpenFOAM.
10
11  OpenFOAM is free software: you can redistribute it and/or modify it
12  under the terms of the GNU General Public License as published by
13  the Free Software Foundation, either version 3 of the License, or
14  (at your option) any later version.
15
16  OpenFOAM is distributed in the hope that it will be useful, but WITHOUT
17  ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or
18  FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License
19  for more details.
20
21  You should have received a copy of the GNU General Public License
22  along with OpenFOAM. If not, see <http://www.gnu.org/licenses/>.
23
24  Class
25  Foam::LogLawShearStress
26
27  Description
28  Aerodynamic entrainment of bed particles
29
30
31  /*-----*\
32
33  #ifndef LogLawShearStress_H
34  #define LogLawShearStress_H
35
36  #include "BedAerodynamicLiftInjectionModel.H"
37
38  // * * * * *
39
40  namespace Foam
41  {
42  /*-----*\
43  Class LogLawShearStress Declaration
44  /*-----*\
45
46  template<class CloudType>
47  class LogLawShearStress
48  :
49  public BedAerodynamicLiftInjectionModel<CloudType>
50  {
51  // Private Data
52
53  //- Mean particle diameter
54  scalar dm_;
55
56  //- Minimum number of particles per parcel
57  scalar pppMin_;
```

Figure 7: LogLawShearStress.H, lines 1 to 57.

```

58
59     //- Std deviation of particle diameter
60     scalar ds_;
61
62     //- Std deviation of particle diameter
63     scalar d_max_;
64
65     //- Std deviation of particle diameter
66     scalar d_min_;
67
68     //- Aerodynamic roughness length
69     scalar z0_;
70
71     //-Start of Activation (launch of saltation)
72     scalar SOA_;
73
74     //-A constant for shear stress threshold computation
75     scalar Acst_;
76
77     //- Number of parcels aerodynamically lifted
78     volScalarField nAeroLift_;
79
80     //- Patch name
81     const word patchName_;
82
83     //- Flag to compute surface shear stress with log-law
84     Switch tauLogLaw_;
85
86     //- Patch ID
87     const label patchId_;
88
89
90 protected:
91
92     // Protected Data
93
94     //- Convenience typedef to the cloud's parcel type
95     typedef typename CloudType::parcelType parcelType;
96
97     //- Parcel size distribution model
98     const autoPtr<distributionModelsTriple::distributionModelTriple>
99     sizeDistributionTriple_;
100
101     // Protected Member Functions
102
103     //- Main aerodynamic entrainment routine
104     virtual void bedAeroLiftInject();
105     void normalInject(const vector& U_NewP, const vector& coord, const vector&
106     coordr, const scalar& d_g, const scalar& nParticle);
107
108     //- Aerodynamically lifted parcel type label - id assigned to identify
109     parcel for
110     // post-processing.
111     label aeroLiftParcelType_;
112
113 public:

```

Figure 8: LogLawShearStress.H, lines 58 to 111.

```

112     //- Runtime type information
113     TypeName("logLawShearStress");
114
115
116     // Constructors
117
118     //- Construct from dictionary
119     LogLawShearStress
120     (
121         const dictionary& dict,
122         CloudType& cloud,
123         const word& modelName = typeName
124     );
125
126     //- Construct copy
127     LogLawShearStress(LogLawShearStress<CloudType>& cm);
128
129     //- Construct and return a clone
130     virtual autoPtr<BedAerodynamicLiftInjectionModel<CloudType> > clone() //const
131     {
132         return autoPtr<BedAerodynamicLiftInjectionModel<CloudType> >
133         (
134             new LogLawShearStress<CloudType>(*this)
135         );
136     }
137
138
139     //- Destructor
140     virtual ~LogLawShearStress();
141
142     // Member Functions
143 };
144
145
146 // * * * * *
147
148 } // End namespace Foam
149
150 // * * * * *
151
152 #ifndef NoRepository
153 # include "LogLawShearStress.C"
154 #endif
155
156 // * * * * *
157
158 #endif
159
160 // *****
161

```

Figure 9: LogLawShearStress.H, lines 112 to 161.

## Implementation of a snow transport model in OpenFOAM

```
1  /*-----*\
2  =====
3  \\      /  F ield      |  OpenFOAM: The Open Source CFD Toolbox
4  \\      /  O peration  |
5  \\      /  A nd        |  Copyright (C) 2011-2013 OpenFOAM Foundation
6  \\      /  M anipulation |
7  -----*\
8  License
9  This file is part of OpenFOAM.
10
11  OpenFOAM is free software: you can redistribute it and/or modify it
12  under the terms of the GNU General Public License as published by
13  the Free Software Foundation, either version 3 of the License, or
14  (at your option) any later version.
15
16  OpenFOAM is distributed in the hope that it will be useful, but WITHOUT
17  ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or
18  FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License
19  for more details.
20
21  You should have received a copy of the GNU General Public License
22  along with OpenFOAM. If not, see <http://www.gnu.org/licenses/>.
23
24  \*-----*/
25
26 #include "LogLawShearStress.H"
27 #include "mathematicalConstants.H"
28 #include "meshTools.H"
29 #include "polyMeshTetDecomposition.H"
30 #include "turbulenceModel.H"
31
32 using namespace Foam::constant::mathematical;
33
34 // * * * * * Protected Member Functions * * * * * //
35 template<class CloudType>
36 void Foam::LogLawShearStress<CloudType>::bedAeroLiftInject()
37 {
38     const fvMesh& mesh = this->owner().mesh();
39     if(mesh.time().value() < SOA_)
40     {
41         // not in the time range: go back
42         return;
43     }
44
45     //////////////////////////////////////
46
47     const volVectorField& U = this->owner().U();
48     const volScalarField& rho = this->owner().rho();
49
50     ////////////////////////////////////// SHEAR STRESS COMPUTATION: GENERAL METHOD
51     const objectRegistry& obr = this->owner().mesh();
52     const turbulenceModel& turbModel = obr.lookupObject<turbulenceModel>
53     (
54         IObject::groupName
55         (
56             turbulenceModel::propertiesName,
57             this->owner().U().group()

```

Figure 10: LogLawShearStress.C, lines 1 to 57.

```

58     )
59 );
60 volScalarField nuEff(turbModel.nuEff());
61
62 volScalarField uFric
63 (
64     IObject
65     (
66         "uFric",
67         this->owner().db().time().timeName(),
68         this->owner().mesh(),
69         IObject::NO_READ,
70         IObject::NO_WRITE
71     ),
72     this->owner().mesh(),
73     dimensionedScalar("uFric", dimVelocity, 0.0)
74 );
75
76 uFric.boundaryField()[patchId_] =
77     sqrt
78     (
79         nuEff.boundaryField()[patchId_]
80         *mag(U.boundaryField()[patchId_].snGrad())
81     );
82 const scalarField& uFp = uFric.boundaryField()[patchId_];
83 const scalarField& y = turbModel.y()[patchId_];
84 const fvPatchVectorField& Uw = turbModel.U().boundaryField()[patchId_];
85 const scalarField magUp(mag(Uw.patchInternalField() - Uw));
86
87 ////////////////////////////////////////////////////
88
89
90 //To access the mesh information for the boundary at target patch patchId_
91 const polyPatch& cPatch = mesh.boundaryMesh()[patchId_];
92
93 //List of cells close to a boundary
94 const labelUList& faceCells = cPatch.faceCells();
95
96 forAll(faceCells, faceI)
97 {
98     label cellInd = faceCells[faceI];
99
100     //COMPUTE SURFACE SHEAR STRESS FROM EULERIAN GRID FOR A GIVEN CELL
101     vector coorC = mesh.C()[cellInd];
102     vector coorf = mesh.Cf().boundaryField()[patchId_][faceI];
103
104     const vector UCell=U[cellInd];
105     const scalar rhoCell=rho[cellInd];
106
107     vector n =
108         -mesh.Sf().boundaryField()[patchId_][faceI]/mesh.magSf().boundaryField()[patch
109         Id_][faceI];
110     vector Un = (UCell & n)*n;
111
112     vector Ut1 = UCell - Un;
113     vector t1 = Ut1/mag(Ut1);
114

```

Figure 11: LogLawShearStress.C, lines 58 to 112.

## Implementation of a snow transport model in OpenFOAM

```

113     vector t2 = t1^n; ///... normal to impacting plane
114
115     scalar cellCentreDistanceToWall = mag((coorC-coorf) & n);
116
117     // OPTIONS FOR SHEAR STRESS COMPUTATION:
118     scalar oldMassCheckPatterns =
119     this->owner().massCheckPatterns().oldTime().boundaryField()[patchId_][faceI];
120
121     scalar tauSurface;
122
123     if(tauLogLaw_)
124     {
125         tauSurface =
126         rhoCell*pow((0.41*mag(Ut1)/(log(cellCentreDistanceToWall/z0_))),2);
127         //log law method, z corresponds to height at center of the face
128     }
129     else
130     {
131         tauSurface = rhoCell*pow(uFp[faceI],2); //To estimate the shear stress
132         as the main method consistent with all the wall function used for
133         nut
134     }
135
136     scalar tauThresh =
137     (Acst_*Acst_)*9.81*dm_*(this->owner().constProps().rho0()-rhoCell); //Shear
138     Stress Threshold (Bagnold).
139     scalar tauExcess = max(0.0,(tauSurface-tauThresh));
140
141     scalar cellArea = mesh.magSf().boundaryField()[patchId_][faceI];
142     scalar nEntrain =
143     1.5*tauExcess/(8.0*constant::mathematical::pi*pow(dm_,2.0)); //Sharma's
144     paper, p.3 - Nae variable
145     nEntrain=nEntrain*cellArea*this->owner().db().time().deltaTValue();
146
147     nAeroLift_.boundaryField()[patchId_][faceI] += nEntrain;
148     scalar entrainment = nAeroLift_.boundaryField()[patchId_][faceI];
149
150     if(entrainment>pppMin_)
151     {//2
152     scalar tempMass =
153     entrainment*this->owner().constProps().rho0()*constant::mathematical::pi*p
154     ow(dm_,3.0)/6.0;
155     scalar depMass =
156     (this->owner().massDeposition().boundaryField()[patchId_][faceI])*cellArea
157     ;
158
159     if(tempMass>depMass)
160     {
161         tempMass=depMass;
162     }
163
164     if(tempMass>0) //If there is still mass to lift up.
165     {//3
166     scalar h_ang = 0.0;
167
168     scalar d_g = sizeDistributionTriple_->logNormalSample(dm_,ds_);
169     d_g = min(d_max_,max(d_g,d_min_));

```

Figure 12: LogLawShearStress.C, lines 113 to 156.

## Implementation of a snow transport model in OpenFOAM

```

157
158         scalar mass_g
           =this->owner().constProps().rho0()*constant::mathematical::pi*pow(d_g, 3)/6.0;
159         scalar entrainmentModified=tempMass/mass_g;
160         label np1 = label(entrainmentModified/pppMin_)+1; //This is because
           last parcel won't be filled up to maximum.
161
162         scalar slope = 0.0;
163         for(label ipl=1; ipl<=np1; ipl++)
164         {
165             scalar nParticle=pppMin_;
166             if(ipl==np1) //If the number of parcels is not the last one,
               which might not be completely full
167             {
168                 nParticle=entrainmentModified-(np1-1)*pppMin_;
169             }
170
171             scalar mean =
               (75.0-55.0*(1.0-exp(-d_g/(175e-6))))/180.0*constant::mathematical::pi;
172             scalar std = 15.0/180.0*constant::mathematical::pi;
173
174             //Vertical angle
175             scalar v_ang = sizeDistributionTriple_->logNormalSample(mean,std);
176             v_ang = min(constant::mathematical::piByTwo,
               max(-constant::mathematical::piByTwo, v_ang+slope));
177
178             scalar vel_fric = sqrt(tauSurface/rhoCell);
179             mean = 3.5*vel_fric;
180             std = 2.5*vel_fric;
181             scalar e_vel = sizeDistributionTriple_->logNormalSample(mean,std);
182
183             vector Un_NewP = (e_vel*sin(v_ang))*n;
184             vector Ut1_NewP = (e_vel*cos(v_ang)*cos(h_ang))*t1;
185             vector Ut2_NewP = (e_vel*cos(v_ang)*sin(h_ang))*t2;
186             vector U_NewP = Un_NewP+Ut1_NewP+Ut2_NewP;
187
188             normalInject(U_NewP,coorC,coorf+(4.0*dm_)*n, d_g, nParticle);
189
190         }
191         this->owner().massDeposition().boundaryField()[patchId_][faceI] -=
           tempMass/cellArea;
192         this->owner().massCheckPatterns().boundaryField()[patchId_][faceI]
           -= tempMass/cellArea;
193         this->owner().surfaceUfric().boundaryField()[patchId_][faceI] =
           uFp[faceI];
194
195     }
196     nAeroLift_.boundaryField()[patchId_][faceI] = 0.0;
197 }
198 this->owner().massDepRate().boundaryField()[patchId_][faceI] =
   (((this->owner().massCheckPatterns().boundaryField()[patchId_][faceI])-oldMassC
   heckPatterns)/(this->owner().db().time().deltaTValue()));
199 }
200 }
201

```

Figure 13: LogLawShearStress.C, lines 157 to 201.



```

202 template<class CloudType>
203 void Foam::LogLawShearStress<CloudType>::normalInject(const vector& U_NewP, const
vector& coorf, const vector& coorfr, const scalar& d_g, const scalar& nParticle)
204 {
205     label cellI = -1;
206     label tetFaceI = -1;
207     label tetPtI = -1;
208     vector pos = coorf;
209     label posInList = -1;
210     this->owner().mesh().findCellFacePt
211     (
212         pos,
213         cellI,
214         tetFaceI,
215         tetPtI
216     );
217
218     if (cellI > -1)
219     {
220         parcelType* pPtr = new parcelType(this->owner().mesh(), coorfr, cellI,
tetFaceI, tetPtI);
221
222         //Check/set new parcel thermo properties
223         this->owner().setParcelThermoProperties(*pPtr, 0.0);
224
225         pPtr->d()=d_g; //assigning the diameter, same for all particles in the parcel
226
227         //Check/set new parcel injection properties
228         this->owner().checkParcelProperties(*pPtr,
this->owner().mesh().time().deltaTValue(), false);
229         pPtr->nParticle()=nParticle;
230
231         pPtr->U()=U_NewP; //assigning the ejection linear velocity
232         pPtr->typeId() = aeroLiftParcelType_;
233
234         // Apply corrections to position for 2-D cases
235         meshTools::constrainToMeshCentre(this->owner().mesh(), pPtr->position());
236
237         // Apply correction to velocity for 2-D cases
238         meshTools::constrainDirection
239         (
240             this->owner().mesh(),
241             this->owner().mesh().solutionD(),
242             pPtr->U()
243         );
244
245         this->owner().addParticle(pPtr);
246     }
247     else
248     {
249         Info << "ERROR: The cell index is negative ... coorf/cellI/tetFaceI/tetPtI"
<< coorf << ' ' << cellI << ' ' << tetFaceI << ' ' << tetPtI << endl;
250     }
251 }
252
253 // * * * * * Constructors * * * * *
254

```

Figure 14: LogLawShearStress.C, lines 202 to 254.

```

255 template<class CloudType>
256 Foam::LogLawShearStress<CloudType>::LogLawShearStress
257 (
258     const dictionary& dict,
259     CloudType& owner,
260     const word& modelName
261 )
262 :
263     BedAerodynamicLiftInjectionModel<CloudType>(dict, owner, modelName),
264     dm_(0.0),
265     ds_(0.0),
266     pppMin_(0.0),
267     d_max_(0.0),
268     d_min_(0.0),
269     z0_(0.0),
270     SOA_(0.0),
271     Acst_(0.0),
272     aeroLiftParcelType_
273     (
274         this->coeffDict().lookupOrDefault("aeroLiftParcelType", 2)
275     ),
276     nAeroLift_
277     (
278         IObject
279         (
280             this->owner().name() + ":nAeroLift",
281             this->owner().db().time().timeName(),
282             this->owner().mesh(),
283             IObject::READ_IF_PRESENT,
284             IObject::NO_WRITE
285         ),
286         this->owner().mesh(),
287         dimensionedScalar("zero", dimless, 0.0), //Number of particles already entrained
288         zeroGradientFvPatchScalarField::typeName //For post-processing purposes
289     ),
290     sizeDistributionTriple_
291     (
292         distributionModelsTriple::distributionModelTriple::New
293         (
294             this->coeffDict().subDict("sizeDistributionTriple"),
295             this->owner().rndGen()
296         )
297     ),
298     patchName_(this->coeffDict().lookup("aerodynamicLiftPatch")),
299     tauLogLaw_(this->coeffDict().lookupOrDefault("tauLogLaw", false)),
300     patchId_(this->owner().mesh().boundaryMesh().findPatchID(patchName_))
301 {
302     if (patchId_ < 0)
303     {
304         FatalErrorIn
305         (
306             "Foam::LogLawShearStress<CloudType>::LogLawShearStress"
307             "("
308             "const dictionary& dict,"
309             "CloudType& owner,"
310             "const word& modelName"

```

Figure 15: LogLawShearStress.C, lines 255 to 310.

```

311     )"
312     ) << "Requested patch " << patchName_ << " not found" << nl
313     << "Available patches are: " << this->owner().mesh().boundaryMesh().names()
314     << nl << exit(FatalError);
315 }
316
317 dm_ = this->coeffDict().lookupOrDefault("dm", 0.00026);
318 ds_ = this->coeffDict().lookupOrDefault("ds", 0.00013);
319 pppMin_ = this->coeffDict().lookupOrDefault("pppMin", 1000);
320 d_max_ = this->coeffDict().lookupOrDefault("d_max", 0.002);
321 d_min_ = this->coeffDict().lookupOrDefault("d_min", 0.00005);
322 z0_ = this->coeffDict().lookupOrDefault("z0", 0.0001);
323 SOA_ = this->coeffDict().lookupOrDefault("SOA", 100.0);
324 Acst_ = this->coeffDict().lookupOrDefault("Acst", 0.1);
325 }
326
327
328 template<class CloudType>
329 Foam::LogLawShearStress<CloudType>::LogLawShearStress
330 (
331     LogLawShearStress<CloudType>& cm
332 )
333 :
334     BedAerodynamicLiftInjectionModel<CloudType>(cm),
335     sizeDistributionTriple_(cm.sizeDistributionTriple_.clone().ptr()),
336     dm_(cm.dm_),
337     ds_(cm.ds_),
338     pppMin_(cm.pppMin_),
339     d_max_(cm.d_max_),
340     d_min_(cm.d_min_),
341     z0_(cm.z0_),
342     SOA_(cm.SOA_),
343     Acst_(cm.Acst_),
344     aeroLiftParcelType_(cm.aeroLiftParcelType_),
345     nAeroLift_(cm.nAeroLift_),
346     patchName_(cm.patchName_),
347     tauLogLaw_(cm.tauLogLaw_),
348     patchId_(cm.patchId_)
349 {
350 }
351 }
352
353
354 // * * * * * Destructor * * * * * //
355
356 template<class CloudType>
357 Foam::LogLawShearStress<CloudType>::~LogLawShearStress()
358 {}
359
360
361 // ***** //
362

```

Figure 16: LogLawShearStress.C, lines 311 to 362.

### 3.2.4 Linking libraries

As a final step, the new BedAerodynamicLiftInjectionModel submodel needs to be linked to the kinematicCloud and parcel classes for compilation purposes. To do so, go to the KinematicCloud directory located at:

```
$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/intermediateCRYOS/...  
clouds/Templates/KinematicCloud
```

Inside this directory, open the `KinematicCloud.C`, `KinematicCloud.H` and `KinematicCloudI.H` files. There, search for the "stochasticCollision" term and copy each line of code containing it, but with replacing every instance of it by "BedAerodynamicLiftInjection". The new submodel also needs to be linked to the parcel object. Using the same first line than the previous path, go to

```
...parcels/include
```

and create a file `makeKinematicParcelBedAerodynamicLiftInjectionModels.H` similarly to the one related to the stochastic collision submodel, named `makeParcelStochasticCollisionModels.H`.

Next, go to

```
...parcels/derived
```

and in the `makeBasic*ParcelSubmodels.C` files of each subfolder, add the reference to the \*.H file created above, just as the other submodels. Because the `StochasticCollision` model served as a template for our aerodynamic lift model, they should appear in the exact same places: this can provide guidance for adding the `BedAerodynamicLiftInjectionModel` submodel in the appropriate files.

### 3.3 Submodel 2: rebound-splash entrainment

#### 3.3.1 Copying the template

The first step in the implementation of the rebound-splash submodel is to make a copy of the `localInteraction` submodel located at the following path:

```
$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/intermediateCRYOS/submodels/...  
Kinematic/PatchInteractionModel/LocalInteraction
```

Once the folder has been copied, follow the subsequent steps:

1. Rename the `LocalInteraction` directory by `LocalInteractionReboundingSplashing`;
2. In the the files contained within, replace every instance of the term "LocalInteraction" by "LocalInteractionStickReboundSplash", and the term "patchInteraction" by "patchInteractionStickReboundSplash";

3. In the file `LocalInteractionStickReboundSplash.C`, go to the `correct()` function and copy the switch case called `itRebound`. Replace the term "itRebound" by "itStickReboundSplash". It is in this case that the rebounding-splashing equations are implemented.

Both the rebound and splash-related equations are included in this submodel.

### 3.3.2 Implementation of rebound equations

The first part of the implemented submodel is related to the rebounding of grains. It is described in section S.1.4.2 from the work of [Sharma et al. \(2018\)](#) and relates to the definition of the probability of rebound defined in Eq.5. It is implemented at the beginning of the `itStickReboundSplash` case switch, at lines 312 - 339 of the `LocalInteractionStickReboundSplash.C` file (see Fig. 25 and 26). The adopted approach is that once a particle gets close to the boundary, a random number is generated and compared to  $P_r$ . If it is within the probability range, the particle is kept and assumed to rebound. If not, it is removed from the numerical domain.

### 3.3.3 Implementation of splash equations

The second part of the submodel is related to the ejection (splashing) of grains due to the effect of particles impacting the surface. It is implemented after the rebound of particles in the `itStickReboundSplash` case, at lines 340 - 442. Line 358 (Fig.26) of the code refers to the energy-related number of ejected particles  $N_E$  (Eq.6) while line 359 refers to the momentum-related one,  $N_M$  (Eq.7). Both of these equations are used to determine the number of splashed particles (line 360). The lines located after relate to the random sampling of the particle properties and the generation of parcels, until line 442 (Fig.28).

### 3.3.4 OpenFOAM scripts

Figures 17 to 19 display the content of the `LocalInteractionStickReboundSplash.H` file which defines the data and functions used in the script. On the other hand, Figures 20 to 30 show the `LocalInteractionStickReboundSplash.C` script. The variables employed in the code should also be added within the `patchInteractionStickReboundSplashData.*` files (not displayed in this tutorial).

```

1  /*-----*\
2  =====
3  \ \ / / F i e l d | OpenFOAM: The Open Source CFD Toolbox
4  \ \ / / O p e r a t i o n |
5  \ \ / / A n d | Copyright (C) 2011-2012 OpenFOAM Foundation
6  \ \ / / M a n i p u l a t i o n |
7  -----*\
8  License
9      This file is part of OpenFOAM.
10
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12     under the terms of the GNU General Public License as published by
13     the Free Software Foundation, either version 3 of the License, or
14     (at your option) any later version.
15
16     OpenFOAM is distributed in the hope that it will be useful, but WITHOUT
17     ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or
18     FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License
19     for more details.
20
21     You should have received a copy of the GNU General Public License
22     along with OpenFOAM. If not, see <http://www.gnu.org/licenses/>.
23
24  Class
25      Foam::LocalInteractionStickReboundSplash
26
27  Description
28      Patch interaction specified on a patch-by-patch basis
29
30  /*-----*\
31
32  #ifndef LocalInteractionStickReboundSplash_H
33  #define LocalInteractionStickReboundSplash_H
34
35  #include "PatchInteractionModel.H"
36  #include "patchInteractionStickReboundSplashDataList.H"
37  #include "Switch.H"
38  #include "distributionModelTriple.H"
39  #include "Random.H"
40
41
42  // * * * * *
43
44  namespace Foam
45  {
46  /*-----*\
47      Class LocalInteractionStickReboundSplash Declaration
48  /*-----*\
49
50  template<class CloudType>
51  class LocalInteractionStickReboundSplash
52  :
53  public PatchInteractionModel<CloudType>
54  {
55  // Private data
56
57      //- List of participating patches

```

Figure 17: LocalInteractionStickReboundSplash.H, lines 1 to 57.

```

58     const patchInteractionStickReboundSplashDataList patchData_;
59
60
61     // Counters for particle fates
62
63     //- Number of parcels escaped
64     List<label> nEscape_;
65
66     //- Mass of parcels escaped
67     List<scalar> massEscape_;
68
69     //- Number of parcels stuck to patches
70     List<label> nStick_;
71
72     //- Mass of parcels stuck to patches
73     List<scalar> massStick_;
74
75     //- Flag to output data as fields
76     Switch writeFields_;
77
78     //- Mass escape field
79     autoPtr<volScalarField> massEscapePtr_;
80
81     //- Mass stick field
82     autoPtr<volScalarField> massStickPtr_;
83
84     //- Mass deposition field
85     //autoPtr<volScalarField> massDepositionPtr_;
86
87 protected:
88
89     //- Convenience typedef to the cloud's parcel type
90     typedef typename CloudType::parcelType parcelType;
91
92     //- Parcel size distribution model
93     const autoPtr<distributionModelsTriple::distributionModelTriple>
94     sizeDistributionTriple_;
95
96 public:
97     //- Runtime type information
98     TypeName("localInteractionStickReboundSplash");
99
100
101     // Constructors
102
103     //- Construct from dictionary
104     LocalInteractionStickReboundSplash(const dictionary& dict, CloudType& owner);
105
106     //- Construct copy from owner cloud and patch interaction model
107     LocalInteractionStickReboundSplash(const
108     LocalInteractionStickReboundSplash<CloudType>& pim);
109
110     //- Construct and return a clone using supplied owner cloud
111     virtual autoPtr<PatchInteractionModel<CloudType> > clone() const
112     {
113         return autoPtr<PatchInteractionModel<CloudType> >

```

Figure 18: LocalInteractionStickReboundSplash.H, lines 58 to 112.

```

113         (
114             new LocalInteractionStickReboundSplash<CloudType>(*this)
115         );
116     };
117
118
119     //- Destructor
120     virtual ~LocalInteractionStickReboundSplash();
121
122
123     // Member Functions
124
125     //- Return access to the massEscape field
126     volScalarField& massEscape();
127
128     //- Return access to the massStick field
129     volScalarField& massStick();
130
131     //- Return access to the massDeposition field
132     //volScalarField& massDeposition();
133
134     //- Apply velocity correction
135     // Returns true if particle remains in same cell
136     virtual bool correct
137     (
138         typename CloudType::parcelType& p,
139         const polyPatch& pp,
140         bool& keepParticle,
141         const scalar trackFraction,
142         const tetIndices& tetIs
143     );
144
145     // I-0
146
147     //- Write patch interaction info to stream
148     virtual void info(Ostream& os);
149 };
150
151
152 // * * * * *
153
154 } // End namespace Foam
155
156 // * * * * *
157
158 #ifdef NoRepository
159 # include "LocalInteractionStickReboundSplash.C"
160 #endif
161
162 // * * * * *
163
164 #endif
165
166 // *****
    
```

Figure 19: LocalInteractionStickReboundSplash.H, lines 113 to 166.



## Implementation of a snow transport model in OpenFOAM

```
1  /*-----*\
2  =====
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5  \ \ / / A n d               |   Copyright (C) 2011-2014 OpenFOAM Foundation
6  \ \ / / M a n i p u l a t i o n |
7  -----*\
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12     under the terms of the GNU General Public License as published by
13     the Free Software Foundation, either version 3 of the License, or
14     (at your option) any later version.
15
16     OpenFOAM is distributed in the hope that it will be useful, but WITHOUT
17     ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or
18     FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License
19     for more details.
20
21     You should have received a copy of the GNU General Public License
22     along with OpenFOAM. If not, see <http://www.gnu.org/licenses/>.
23
24  /*-----*\
25
26  #include "LocalInteractionStickReboundSplash.H"
27  #include "mathematicalConstants.H"
28  #include "meshTools.H"
29
30  // * * * * * Constructors * * * * * //
31
32  template<class CloudType>
33  Foam::LocalInteractionStickReboundSplash<CloudType>::LocalInteractionStickReboundSplā
34  ash
35  (
36      const dictionary& dict,
37      CloudType& cloud
38  )
39  :
40      PatchInteractionModel<CloudType>(dict, cloud, typeName),
41      patchData_(cloud.mesh(), this->coeffDict()),
42      nEscape_(patchData_.size(), 0),
43      massEscape_(patchData_.size(), 0.0),
44      nStick_(patchData_.size(), 0),
45      massStick_(patchData_.size(), 0.0),
46      writeFields_(this->coeffDict().lookupOrDefault("writeFields", true)),
47      massEscapePtr_(NULL),
48      massStickPtr_(NULL),
49      sizeDistributionTriple_
50      (
51          distributionModelsTriple::distributionModelTriple::New
52          (
53              this->coeffDict().subDict("sizeDistributionTriple"),
54              this->owner().rndGen()
55          )
56      )
57  {
```

Figure 20: LocalInteractionStickReboundSplash.C, lines 1 to 56.

```

57     if (writeFields_)
58     {
59         word massEscapeName(this->owner().name() + ":massEscape");
60         word massStickName(this->owner().name() + ":massStick");
61         Info<< "      Interaction fields will be written to " << massEscapeName << ", "
62         << " and " << massStickName << endl;
63
64         (void)massEscape();
65         (void)massStick();
66     }
67     else
68     {
69         Info<< "      Interaction fields will not be written" << endl;
70     }
71
72     // check that interactions are valid/specified
73     forAll(patchData_, patchI)
74     {
75         const word& interactionTypeName =
76             patchData_[patchI].interactionTypeName();
77         const typename PatchInteractionModel<CloudType>::interactionType& it =
78             this->wordToInteractionType(interactionTypeName);
79
80         if (it == PatchInteractionModel<CloudType>::itOther)
81         {
82             const word& patchName = patchData_[patchI].patchName();
83             FatalErrorIn("LocalInteractionStickReboundSplash(const dictionary&,
84                 CloudType&)"
85                 << "Unknown patch interaction type "
86                 << interactionTypeName << " for patch " << patchName
87                 << ". Valid selections are:"
88                 << this->PatchInteractionModel<CloudType>::interactionTypeNames_
89                 << nl << exit(FatalError);
90         }
91     }
92
93
94     template<class CloudType>
95     Foam::LocalInteractionStickReboundSplash<CloudType>::LocalInteractionStickReboundSpl
96     ash
97     (
98         const LocalInteractionStickReboundSplash<CloudType>& pim
99     )
100    :
101    PatchInteractionModel<CloudType>(pim),
102    patchData_(pim.patchData_),
103    nEscape_(pim.nEscape_),
104    massEscape_(pim.massEscape_),
105    nStick_(pim.nStick_),
106    massStick_(pim.massStick_),
107    writeFields_(pim.writeFields_),
108    massEscapePtr_(NULL),
109    massStickPtr_(NULL),
110    sizeDistributionTriple_(pim.sizeDistributionTriple_().clone().ptr())
111    {}

```

Figure 21: LocalInteractionStickReboundSplash.C, lines 57 to 111.

```

112
113 // * * * * * D e s t r u c t o r * * * * * //
114
115 template<class CloudType>
116 Foam::LocalInteractionStickReboundSplash<CloudType>::~LocalInteractionStickReboundSp
lash()
117 {
118
119
120 // * * * * * M e m b e r F u n c t i o n s * * * * * //
121
122 template<class CloudType>
123 Foam::volScalarField&
Foam::LocalInteractionStickReboundSplash<CloudType>::massEscape()
124 {
125     if (!massEscapePtr_.valid())
126     {
127         const fvMesh& mesh = this->owner().mesh();
128
129         massEscapePtr_.reset
130         (
131             new volScalarField
132             (
133                 IObject
134                 (
135                     this->owner().name() + ":massEscape",
136                     mesh.time().timeName(),
137                     mesh,
138                     IObject::READ_IF_PRESENT,
139                     IObject::AUTO_WRITE
140                 ),
141                 mesh,
142                 dimensionedScalar("zero", dimMass, 0.0)
143             )
144         );
145     }
146
147     return massEscapePtr_();
148 }
149
150
151 template<class CloudType>
152 Foam::volScalarField&
Foam::LocalInteractionStickReboundSplash<CloudType>::massStick()
153 {
154     if (!massStickPtr_.valid())
155     {
156         const fvMesh& mesh = this->owner().mesh();
157
158         massStickPtr_.reset
159         (
160             new volScalarField
161             (
162                 IObject
163                 (
164                     this->owner().name() + ":massStick",
165                     mesh.time().timeName(),

```

Figure 22: LocalInteractionStickReboundSplash.C, lines 112 to 165.

```

166         mesh,
167         IObject::READ_IF_PRESENT,
168         IObject::AUTO_WRITE
169     ),
170     mesh,
171     dimensionedScalar("zero", dimMass, 0.0)
172 );
173 );
174 }
175
176 return massStickPtr_();
177 }
178
179 template<class CloudType>
180 bool Foam::LocalInteractionStickReboundSplash<CloudType>::correct
181 (
182     typename CloudType::parcelType& p,
183     const polyPatch& pp,
184     bool& keepParticle,
185     const scalar trackFraction,
186     const tetIndices& tetIs
187 )
188 {
189     label patchI = patchData_.applyToPatch(pp.index());
190
191     if (patchI >= 0)
192     {
193         vector& U = p.U();
194         bool& active = p.active();
195
196         typename PatchInteractionModel<CloudType>::interactionType it =
197             this->wordToInteractionType
198             (
199                 patchData_[patchI].interactionTypeName()
200             );
201
202         switch (it)
203         {
204             case PatchInteractionModel<CloudType>::itEscape:
205             {
206                 scalar dm = p.mass()*p.nParticle();
207
208                 keepParticle = false;
209                 active = false;
210                 U = vector::zero;
211                 nEscape_[patchI]++;
212                 massEscape_[patchI] += dm;
213                 if (writeFields_)
214                 {
215                     label pI = pp.index();
216                     label fI = pp.whichFace(p.face());
217                     massEscape().boundaryField()[pI][fI] += dm;
218                 }
219                 break;
220             }
221             case PatchInteractionModel<CloudType>::itStick:
222             {

```

Figure 23: LocalInteractionStickReboundSplash.C, lines 166 to 222.

```

223         scalar dm = p.mass()*p.nParticle();
224
225         keepParticle = true;
226         active = false;
227         U = vector::zero;
228         nStick_[patchI]++;
229         massStick_[patchI] += dm;
230         if (writeFields_)
231         {
232             label pI = pp.index();
233             label fI = pp.whichFace(p.face());
234             massStick().boundaryField()[pI][fI] += dm;
235         }
236         break;
237     }
238     case PatchInteractionModel<CloudType>::itRebound:
239     {
240         keepParticle = true;
241         active = true;
242
243         vector nw;
244         vector Up;
245
246         this->owner().patchData(p, pp, trackFraction, tetIs, nw, Up);
247
248         // Calculate motion relative to patch velocity
249         U -= Up;
250
251         scalar Un = U & nw;
252         vector Ut = U - Un*nw;
253
254         if (Un > 0)
255         {
256             U -= (1.0 + patchData_[patchI].e())*Un*nw;
257         }
258
259         U -= patchData_[patchI].mu()*Ut;
260
261         // Return velocity to global space
262         U += Up;
263
264         break;
265     }
266
267     ////////////////////////////////////////
268     ////////////////////////////////////////
269     //CASE SWITCH FOR REBOUND-SPLASH OF SNOW GRAINS
270     case PatchInteractionModel<CloudType>::itStickReboundSplash:
271     {
272         vector nw;
273         vector Up;
274         this->owner().patchData(p, pp, trackFraction, tetIs, nw, Up);
275
276         const fvMesh& mesh = this->owner().mesh();
277         cachedRandom& ranGen = this->owner().rndGen();
278         label pI = pp.index();
279         label fI = pp.whichFace(p.face());
    
```

Figure 24: LocalInteractionStickReboundSplash.C, lines 223 to 277.

## Implementation of a snow transport model in OpenFOAM

```

278         scalar cellArea = mesh.magSf().boundaryField()[pI][fI];
279         label cellInd = mesh.faceOwner()[fI];
280
281         // Calculate motion relative to patch velocity
282         U -= Up;
283
284         vector n = -nw;
285         vector Un = (U & n)*n;
286
287         vector Ut1 = U - Un;
288         vector t1 = Ut1/(mag(Ut1)+ROOTVSMALL);
289
290         vector t2 = t1^n;
291
292         // Impact Properties
293         scalar i_vel = mag(U);
294         scalar n_impact = p.nParticle();           //number of particles  ↵
295         scalar pMassParcel=p.nParticle()*p.mass(); //mass of the parcel
296         scalar i_ene=0.5*pMassParcel*pow(i_vel,2);
297         scalar i_mom=pMassParcel*i_vel;
298
299
300
301
302         scalar i_ang1 = atan(mag(Un)/ (mag(Ut1)+ROOTVSMALL) );
303
304
305         scalar slope = 0.0;
306
307         // i_ang2 is impacting angle with respect to bed surface, or vang  ↵
308         // of impacting particle
309         // To get the horizontal angle with respect to impacting plane,  ↵
310         // must set i_ang2
311
312         i_ang2=0.0;
313
314         // PART I: REBOUNDING OF GRAINS
315         scalar prob_reb= 0.9*(1.0-exp(-2.0*i_vel)); //Probability of  ↵
316         //rebound for particles
317         scalar rand = ranGen.sample01<scalar>();
318         if(rand<prob_reb && (U & n)<=0. )
319         {
320             //Sampling ejection angle from distribution
321             scalar r_vel=0.5*i_vel;
322             scalar mean= 45.0/180*constant::mathematical::pi;
323             scalar v_ang =
324             sizeDistributionTriple_->exponentialSample(mean,0.0);
325             v_ang = min(constant::mathematical::piByTwo,
326             max(-constant::mathematical::piByTwo, v_ang+slope));
327             Un = (r_vel*sin(v_ang))*n;
328             Ut1 = (r_vel*cos(v_ang))*t1;
329             U = Ut1+Un;
330             // Return velocity to global space
331             U += Up;
332             keepParticle = true;
333             active = true;

```

Figure 25: LocalInteractionStickReboundSplash.C, lines 278 to 328.

```

329     }
330     else
331     {
332         //If probability < probability of rebound: back to the snow bed
333         this->owner().massDeposition().boundaryField()[pI][fI] +=
334         (pMassParcel)/cellArea;
335         this->owner().massCheckPatterns().boundaryField()[pI][fI] +=
336         (pMassParcel)/cellArea;
337         keepParticle = false;
338         active = false;
339         U = vector::zero;
340     }
341
342     // PART II: SPLASHING OF GRAINS
343     scalar epsilonf_ = 0.96*(1.0-prob_reb*patchData_[patchI].epsilonf());
344     scalar av_d3=
345     pow(patchData_[patchI].dm()+pow(patchData_[patchI].ds(),2.0)/patchData_
346     ta_[patchI].dm(),3.0);
347     scalar sd_d3 =
348     av_d3*sqrt(pow(1.0+pow(patchData_[patchI].ds()/patchData_[patchI].dm
349     (),2.0),9.0)-1.0);
350     scalar av_vel = 0.25*pow(i_vel,0.3);
351     scalar av_vel2 = 2.0*pow(av_vel,2.0);
352     scalar av_mass = p.rho()*constant::mathematical::pi/6.0*av_d3;
353     scalar sd_vel = av_vel;
354     scalar sd_vel2 = 2.0*sqrt(5.0)*pow(av_vel,2.0);
355     scalar sd_mass = p.rho()*constant::mathematical::pi/6.0*sd_d3;
356
357     scalar cos_a = 0.75;
358     scalar cos_b = 0.96;
359     scalar cos_i = cos(i_ang1);
360
361     scalar av_massvel = av_mass*av_vel*cos_a*cos_b +
362     patchData_[patchI].corr()*sd_mass*sd_vel;
363     scalar av_massvel2 = av_mass*av_vel2 +
364     patchData_[patchI].corre()*sd_mass*sd_vel2;
365     // Number of ejected particles based on energy/momentum
366     conservation (Comola & Lehning, 2017)
367     scalar n_splash1 =
368     i_ene*(1.0-prob_reb*patchData_[patchI].epsilonf() -
369     epsilonf_)/(0.5*av_massvel2+patchData_[patchI].bEne()+ROOTVSMALL);
370     scalar n_splash2 = i_mom*cos_i*(1.0 -
371     prob_reb*patchData_[patchI].mur() -
372     patchData_[patchI].muf())/(av_massvel+ROOTVSMALL);
373     scalar n_splash = min(n_splash1,n_splash2);
374
375     // Sampling of particle properties
376     // Condition: number of splashed particles >= number of impacting
377     particles (model choice)
378     if(n_splash>=n_impact)
379     {
380         // Taking into account an unfilled last parcel
381         label np1 = label(n_splash/patchData_[patchI].pppMax()+1);
382
383         for(label ip1=1; ip1<=np1; ip1++)
384         {
385
386
387
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```

Figure 26: LocalInteractionStickReboundSplash.C, lines 329 to 371.

```

372     scalar d_g =
        sizeDistributionTriple_->logNormalSample(patchData_[patchI].
        dm(),patchData_[patchI].ds());
373     d_g =
        min(patchData_[patchI].d_max(),max(d_g,patchData_[patchI].d_
        min()));
374     scalar mass_g =
        p.rho()*constant::mathematical::pi*pow(d_g,3)/6.0;
375
376     scalar dep_mass =
        (this->owner().massDeposition().boundaryField()[pI][fI])*cel
        lArea;
377     scalar temp_mass = 0.0;
378
379     if(ip1!=np1)
380     {
381         temp_mass = patchData_[patchI].pppMax()*mass_g;
382     }
383     else // Condition for unfilled last parcel
384     {
385         temp_mass =
            (n_splash-(np1-1)*patchData_[patchI].pppMax()*mass_g;
386     }
387
388     if(temp_mass > dep_mass)
389     {
390         temp_mass = dep_mass;
391     }
392
393     if(temp_mass > 0.0) //If negative, no more snow at the
        surface
394     {
395         parcelType* pPtr = new parcelType(mesh,
            p.position(),p.cell(), p.tetFace(), p.tetPt());
396
397         // Check/set new parcel thermo properties
398         this->owner().setParcelThermoProperties(*pPtr, 0.0);
399
400         pPtr->d()=d_g;
401
402         pPtr->nParticle()=temp_mass/mass_g;
403
404         // Check/set new parcel injection properties
405         this->owner().checkParcelProperties(*pPtr,
            0.0*mesh.time().deltaTValue(), false);
406
407         // Random sampling of velocities and angles from
            statistical distributions
408         scalar
            e_vel=sizeDistributionTriple_->exponentialSample(av_vel,0.0)
            ;
409         scalar
            v_ang=sizeDistributionTriple_->exponentialSample(50.0/180.0*
            constant::mathematical::pi,0.0);
410         scalar
            h_ang=sizeDistributionTriple_->normalSample(i_ang2,15.0/180.
            0*constant::mathematical::pi);
    
```

Figure 27: LocalInteractionStickReboundSplash.C, lines 372 to 410.



## Implementation of a snow transport model in OpenFOAM

```

411         h_ang = min(constant::mathematical::pi,
412                    max(-constant::mathematical::pi, h_ang));
413         v_ang = min(constant::mathematical::piByTwo,
414                    max(-constant::mathematical::piByTwo, v_ang+slope));
415
416         vector Un_splashing = (e_vel*sin(v_ang))*n;
417         vector Ut1_splashing = (e_vel*cos(v_ang)*cos(h_ang))*t1;
418         vector Ut2_splashing = (e_vel*cos(v_ang)*sin(h_ang))*t2;
419         vector Ut_splashing =
420             Un_splashing+Ut1_splashing+Ut2_splashing;
421
422         // Return velocity to global space
423         Ut_splashing += Up;
424
425         // Assigning the splashing linear velocity
426         pPtr->U()=Ut_splashing;
427
428         // Apply corrections to position for 2-D cases
429         meshTools::constrainToMeshCentre(mesh, pPtr->position());
430
431         // Apply correction to velocity for 2-D cases
432         meshTools::constrainDirection
433         (
434             mesh,
435             mesh.solutionD(),
436             pPtr->U()
437         );
438         this->owner().addParticle(pPtr);
439         this->owner().massDeposition().boundaryField()[pI][fI] -=
440             temp_mass/cellArea;
441         this->owner().massCheckPatterns().boundaryField()[pI][fI]
442             -=
443             temp_mass/cellArea;
444     }
445 }
446 break;
447 }
448
449 ////////////////////////////////////////////////////
450 ////////////////////////////////////////////////////
451
452 default:
453 {
454     FatalErrorIn
455     (
456         "bool LocalInteractionStickReboundSplash<CloudType>::correct"
457         "("
458         "    typename CloudType::parcelType&, "
459         "    const polyPatch&, "
460         "    bool&, "
461         "    const scalar, "
462         "    const tetIndices&"
463         ") const"
464     )
465     << "Unknown interaction type "
466     << patchData_[patchI].interactionTypeName()
467     << "(" << it << ")" for patch "

```

Figure 28: LocalInteractionStickReboundSplash.C, lines 411 to 459.

```

460         << patchData_[patchI].patchName()
461         << ". Valid selections are:" << this->interactionTypeNames_
462         << endl << abort(FatalError);
463     }
464 }
465
466     return true;
467 }
468
469     return false;
470 }
471
472
473 template<class CloudType>
474 void Foam::LocalInteractionStickReboundSplash<CloudType>::info(Ostream& os)
475 {
476     // retrieve any stored data
477     labelList npe0(patchData_.size(), 0);
478     this->getModelProperty("nEscape", npe0);
479
480     scalarList mpe0(patchData_.size(), 0.0);
481     this->getModelProperty("massEscape", mpe0);
482
483     labelList nps0(patchData_.size(), 0);
484     this->getModelProperty("nStick", nps0);
485
486     scalarList mps0(patchData_.size(), 0.0);
487     this->getModelProperty("massStick", mps0);
488
489     // accumulate current data
490     labelList npe(nEscape_);
491     Pstream::listCombineGather(npe, plusEq0p<label>());
492     npe = npe + npe0;
493
494     scalarList mpe(massEscape_);
495     Pstream::listCombineGather(mpe, plusEq0p<scalar>());
496     mpe = mpe + mpe0;
497
498     labelList nps(nStick_);
499     Pstream::listCombineGather(nps, plusEq0p<label>());
500     nps = nps + nps0;
501
502     scalarList mps(massStick_);
503     Pstream::listCombineGather(mps, plusEq0p<scalar>());
504     mps = mps + mps0;
505
506
507     forAll(patchData_, i)
508     {
509         os << "    Parcel fate (number, mass)      : patch "
510            << patchData_[i].patchName() << nl
511            << "    - escape                                = " << npe[i]
512            << ", " << mpe[i] << nl
513            << "    - stick                                = " << nps[i]
514            << ", " << mps[i] << nl;
515     }
516 }

```

Figure 29: LocalInteractionStickReboundSplash.C, lines 460 to 516.

```

517 |
518 |     if (this->outputTime())
519 |     {
520 |         this->setModelProperty("nEscape", npe);
521 |         nEscape_ = 0;
522 |
523 |         this->setModelProperty("massEscape", mpe);
524 |         massEscape_ = 0.0;
525 |
526 |         this->setModelProperty("nStick", nps);
527 |         nStick_ = 0;
528 |
529 |         this->setModelProperty("massStick", mps);
530 |         massStick_ = 0.0;
531 |     }
532 | }
533 | // ***** //
    
```

Figure 30: LocalInteractionStickReboundSplash.C, lines 517 to 533.

### 3.3.5 Linking libraries

The newly implemented submodel needs to be linked to other classes for compilation purposes. As a first step, the itStickReboundSplash case needs to be added to the PatchInteractionModel. For this purpose, open all the files found at the following path:

```

$WM_PROJECT_USER_DIR/src/lagrangianCRYOS/intermediateCRYOS/submodels/...
Kinematic/PatchInteractionModel/PatchInteractionModel/
    
```

For each document, copy the lines where the term "itStick" appears. Replace the latter by the "itStickReboundSplash" expression to insure that the new switch case is taken into account. In addition, the LocalInteractionStickReboundSplash submodel should be specified in ../intermediateCRYOS/Make/files. For this purpose, all the lines with the term "LocalInteraction" should be copied and the term replaced by "LocalInteractionStickReboundSplash" within them.

## 3.4 Adding a momentum source

### 3.4.1 Definition

A pressure source term  $\mathcal{P}$  was added to the right hand side (RHS) of the flow momentum equations in the DPMFoam solver to drive the motion of the continuous phase. It is a large-scale pressure gradient in the streamwise direction  $x$  described as:

$$\mathcal{P} = -\frac{1}{\rho_f} \frac{\partial \widetilde{p}_\infty}{\partial x} = \frac{u_*^2}{L_z} \quad (8)$$

with  $p$  the pressure,  $u_*$  the surface friction velocity and  $L_z$  the vertical extent of the domain (Sharma et al., 2018). This term was introduced in the `createFields.H` and `UcEqn.H` files both located at:

```
$WM_PROJECT_USER_DIR/applications/solvers/snowDPMFoam/
```

The pressure gradient value is computed within `createFields.H` using the user-defined friction velocity  $u_*$ , flow direction and the height of the domain  $L_z$  as an input. These variables are specified in the `run/case/constant/transportProperties` file. Once the term is computed within `createFields.H`, it is integrated in the momentum equation within `UcEqn.H`.

### 3.4.2 OpenFOAM scripts

The two scripts accounting for the momentum source are presented in this subsection. They also relate to the next section which describes the initial velocity profile settings (sect. 3.5). Figures 31 to 35 show the `createFields.H` file. On the other hand, Figure 36 shows `UcEqn.H`. Lines 170 to 250 of `createFields.H` contain the part that was implemented for the snow transport model. The pressure gradient is computed through several variables (lines 176 - 190) and stored in the `volVectorField` `gradP` (lines 185 to 210). The latter is then inserted on the RHS of the equation in `UcEqn.H` (line 7).

```

1   Info<< "\nReading transportProperties\n" << endl;
2
3   IOdictionary transportProperties
4   (
5       IObject
6       (
7           "transportProperties",
8           runTime.constant(),
9           mesh,
10          IObject::MUST_READ_IF_MODIFIED,
11          IObject::NO_WRITE,
12          false
13      )
14  );
15
16  word contiuousPhaseName(transportProperties.lookup("contiuousPhaseName"));
17
18  dimensionedScalar rhocValue
19  (
20      IObject::groupName("rho", contiuousPhaseName),
21      dimDensity,
22      transportProperties.lookup
23      (
24          IObject::groupName("rho", contiuousPhaseName)
25      )
26  );
27
28  volScalarField rhoc
29  (
30      IObject
31      (
32          rhocValue.name(),
33          runTime.timeName(),
34          mesh,
35          IObject::NO_READ,
36          IObject::AUTO_WRITE
37      ),
38      mesh,
39      rhocValue
40  );
41
42  Info<< "Reading field U\n" << endl;
43  volVectorField Uc
44  (
45      IObject
46      (
47          IObject::groupName("U", contiuousPhaseName),
48          runTime.timeName(),
49          mesh,
50          IObject::MUST_READ,
51          IObject::AUTO_WRITE
52      ),
53      mesh
54  );
55
56  Info<< "Reading field p\n" << endl;
57  volScalarField p

```

Figure 31: createFields.H, lines 1 to 57.

```

58     (
59         IObject
60         (
61             "p",
62             runTime.timeName(),
63             mesh,
64             IObject::MUST_READ,
65             IObject::AUTO_WRITE
66         ),
67         mesh
68     );
69
70
71     Info<< "Reading/calculating continuous-phase face flux field phic\n"
72         << endl;
73
74     surfaceScalarField phic
75     (
76         IObject
77         (
78             IObject::groupName("phi", contiuousPhaseName),
79             runTime.timeName(),
80             mesh,
81             IObject::READ_IF_PRESENT,
82             IObject::AUTO_WRITE
83         ),
84         linearInterpolate(Uc) & mesh.Sf()
85     );
86
87     label pRefCell = 0;
88     scalar pRefValue = 0.0;
89     setRefCell(p, mesh.solutionDict().subDict("PIMPLE"), pRefCell, pRefValue);
90
91     Info<< "Creating turbulence model\n" << endl;
92
93     singlePhaseTransportModel continuousPhaseTransport(Uc, phic);
94
95     volScalarField muc
96     (
97         IObject
98         (
99             IObject::groupName("mu", contiuousPhaseName),
100            runTime.timeName(),
101            mesh,
102            IObject::NO_READ,
103            IObject::AUTO_WRITE
104        ),
105        rhoc*continuousPhaseTransport.nu()
106    );
107
108    Info << "Creating field alphac\n" << endl;
109    // alphac must be constructed before the cloud
110    // so that the drag-models can find it
111    volScalarField alphac
112    (
113        IObject
114        (

```

Figure 32: createFields.H, lines 58 to 114.

```

115         IObject::groupName("alpha", contiuousPhaseName),
116         runTime.timeName(),
117         mesh,
118         IObject::READ_IF_PRESENT,
119         IObject::AUTO_WRITE
120     ),
121     mesh,
122     dimensionedScalar("0", dimless, 0)
123 );
124
125 word kinematicCloudName("kinematicCloud");
126 args.optionReadIfPresent("cloudName", kinematicCloudName);
127
128 Info<< "Constructing kinematicCloud " << kinematicCloudName << endl;
129 basicKinematicTypeCloud kinematicCloud
130 (
131     kinematicCloudName,
132     rhoc,
133     Uc,
134     muc,
135     g
136 );
137
138 // Particle fraction upper limit
139 scalar alphacMin
140 (
141     1.0
142     - readScalar
143     (
144         kinematicCloud.particleProperties().subDict("constantProperties")
145         .lookup("alphaMax")
146     )
147 );
148
149 // Update alphac from the particle locations
150 alphac = max(1.0 - kinematicCloud.theta(), alphacMin);
151 alphac.correctBoundaryConditions();
152
153 surfaceScalarField alphacf("alphacf", fvc::interpolate(alphac));
154 surfaceScalarField alphaPhic("alphaPhic", alphacf*phic);
155
156
157 autoPtr<PhaseIncompressibleTurbulenceModel<singlePhaseTransportModel> >
158 continuousPhaseTurbulence
159 (
160     PhaseIncompressibleTurbulenceModel<singlePhaseTransportModel>::New
161     (
162         alphac,
163         Uc,
164         alphaPhic,
165         phic,
166         continuousPhaseTransport
167     )
168 );
169
170 scalar vKC_ = readScalar(transportProperties.lookup("vKC"));
171 Info << "Reading k_, the Von Kármán constant " << vKC_ << "\n" << endl;

```

Figure 33: createFields.H, lines 115 to 171.

## Implementation of a snow transport model in OpenFOAM

```

172
173 scalar Z0_ = readScalar(transportProperties.lookup("Z0"));
174 Info << "Reading Z0_, the surface roughness, in m " << Z0_ << "\n" << endl;
175
176 scalar Ustar_ = readScalar(transportProperties.lookup("Ustar"));
177 Info << "Reading Ustar_, the friction velocity, in m s-1" << Ustar_ << "\n" << endl;
178
179 scalar H_ = readScalar(transportProperties.lookup("H"));
180 Info << "Reading H_, the height for the fluid domain " << H_ << "\n" << endl;
181
182 vector flowDirection_(transportProperties.lookup("flowDirection"));
183 Info << "Reading flowDirection_, the flow direction " << flowDirection_ << "\n" << endl;
184
185 bool constantPGrad_(transportProperties.lookupOrDefault<bool>("constantPGrad",
186 false));
187 Info << "Reading the flag if constant pressure gradients is applied to momentum ,
188 " << constantPGrad_ << "\n" << endl;
189
190 vector dP_dx = (constantPGrad_ ? (Foam::pow(Ustar_,2.0)/H_)*flowDirection_ :
191 vector::zero);
192 Info << "Calculating the pressure gradient in the flow direction " << dP_dx <<
193 "\n" << endl;
194
195 scalar noiseFactor_ = readScalar(transportProperties.lookup("noiseFactor"));
196 Info << "Reading noiseFactor_, the noise factor " << noiseFactor_ << "\n" << endl;
197
198 const pointField& ctrs = mesh.cellCentres();
199
200 volVectorField gradP
201 (
202     IObject
203     (
204         "gradP",
205         runTime.timeName(),
206         mesh,
207         IObject::NO_READ,
208         IObject::AUTO_WRITE
209     ),
210     mesh,
211     dimensionedVector("gradP", dimForce/dimVolume/dimDensity, dP_dx),
212     zeroGradientFvPatchVectorField::typeName
213 );
214
215 if ( runTime.timeName() == "0" )
216 {
217     Random ranGen_(label(0));
218
219     label totalCellNumber=ctrs.size();
220     reduce(totalCellNumber, sumOp<label>());
221     scalarField randomNumbersAllMesh(totalCellNumber, 0.0);
222     forAll(randomNumbersAllMesh, i)
223     {
224         randomNumbersAllMesh[i]=ranGen_.scalar01();
225     }
226 }

```

Figure 34: createFields.H, lines 172 to 223.



## Implementation of a snow transport model in OpenFOAM

```
224 Info << "\nthe total cell number: " << totalCellNumber << endl << endl;
225
226 labelList LcellN(Pstream::nProcs());
227 LcellN[Pstream::myProcNo()] = ctrs.size();
228 Pstream::gatherList(LcellN);
229 Pstream::scatterList(LcellN);
230
231 label startLable=0;
232 for(label proc=1; proc<=Pstream::myProcNo(); proc++)
233 {
234     startLable+=LcellN[proc-1];
235 }
236
237 Info<< "The streamwise velocity is initialized based on log law at Time = " <<
runTime.timeName() << nl << endl;
238 forAll(ctrs, cellI)
239 {
240     scalar randNumber=randomNumbersAllMesh[cellI+startLable];
241     scalar noise_ = (2.0*randNumber)-1.0;
242     scalar varianceFact_ = 3.0*noiseFactor_*pow(Ustar_,2);
243     scalar cellHeight = ctrs[cellI].z();
244     Uc[cellI] =
        (((Ustar_/vKC_)*Foam::log(cellHeight/Z0_))+varianceFact_*noise_*((H_-0.9*cell
        lHeight)/H_))*flowDirection_;
245     Info << "Uc[cellI]: " << Uc[cellI] << endl;
246
247 }
248 Uc.correctBoundaryConditions();
249 phic=linearInterpolate(Uc) & mesh.Sf();
250 }
```

Figure 35: createFields.H, lines 224 to 250.

```

1 fvVectorMatrix UcEqn
2 (
3     fvm::ddt(alphaC, Uc) + fvm::div(alphaPhic, Uc)
4     - fvm::Sp(fvc::ddt(alphaC) + fvc::div(alphaPhic), Uc)
5     + continuousPhaseTurbulence->divDevRhoReff(Uc)
6     ==
7     gradP
8     + (1.0/rhoc)*cloudSU
9
10 );
11
12 UcEqn.relax();
13
14 volScalarField rAUc(1.0/UcEqn.A());
15 surfaceScalarField rAUcf("Dp", fvc::interpolate(rAUc));
16
17 surfaceScalarField phicForces
18 (
19     (fvc::interpolate(rAUc*cloudVolSUSu/rhoc) & mesh.Sf())
20     +
21     rAUcf*(g & mesh.Sf())
22 );
23
24 if (pimple.momentumPredictor())
25 {
26     solve
27     (
28         UcEqn
29         ==
30         fvc::reconstruct
31         (
32             phicForces/rAUcf - fvc::snGrad(p)*mesh.magSf()
33         )
34     );
35 }

```

Figure 36: UcEqn.H, lines 1 to 35.

### 3.5 Initial velocity profile

In order to reach faster the flow equilibrium, an initial velocity profile is imposed at the beginning of the simulation. It is expected that turbulent eddies lead to an irregular logarithmic law velocity profile. This is taken into account through the `varianceFact_` and `noise_` scalars that add some variability and noise to the theoretical velocity curve (line 244 of `createFields.H`).

### 3.6 Implementation of volScalarField objects

In order to visualize the erosion and deposition of particles occurring at the snow bed as well as the friction velocity, several `volScalarField` objects were inserted directly into the `KinematicCloud` template files (path specified in section 3.2.4). This allows to have objects updated by both the aerodynamic lift and rebound-splash submodels. Note that this particular step requires extra care from the user as changes are brought to the core classes of the

lagrangian library. To add these variables, search the already implemented variable called "Ucoeff" and copy every instance of it in the KinematicCloud.C, KinematicCloud.H and KinematicCloudI.H files. Within the copied text, replace the DimensionedField type by volScalarField. Also bring changes to the units by adding "dimMass/dimArea" for the mass per area objects or "dimVelocity" for the surface friction velocity in the definition of the object. Table 2 summarizes the implemented objects that belong to the volScalarField type.

volScalarField name	Utility
massDeposition	Allows the control of the amount of particles that gets generated within each cell. The available snow mass per surface area is constantly updated when particles get deposited or eroded. A negative value for this object prevents particles from being created in the numerical domain. Occurrence: Figures 13-14 (LogLawShearStress) and 26-27-28 (LocalInteractionStickReboundSplash).
massCheckPatterns	Records cumulatively the mass per unit area that gets eroded and deposited in each cell for the whole simulation. At each time step, this object is updated by both submodels and allows the visualization of the snow distribution patterns resulting from the model. Occurrence: Figures 14 (LogLawShearStress, line 221) and 26-28 (LocalInteractionStickReboundSplash, lines 334 and 437).
massDepRate	Reports the mass deposition/erosion rates per cell at each timestep based on the newly computed massCheckPatterns values and the ones from the previous time step. Occurrence: Figures 14 (LogLawShearStress, line 231).
surfaceUfric	Stores the surface friction velocity computed within each surface cell and which is used within the aerodynamic lift submodel. The friction velocity can be computed in two ways. Occurrence: Figure 14 (LogLawShearStress, line 224).

Table 2: List of the volScalarField objects implemented in OpenFOAM.

## End note

This tutorial shows the main implementation scripts of the new OpenFOAM lagrangian submodels created to simulate the aeolian transport of snow. We refer to this first version of the model as *snowBedFoam 1.0*. The parts of the scripts that were not displayed in the figures (e.g. the KinematicCloud files) can be found within the official repository of the code (WSL-SLF GitLab).

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